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A biomimetic sliding–stretching approach to seismic isolation

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Abstract There is growing demand in industrialized and developing countries to provide people and structures with effective earthquake protection. Here, we employ architectured material concepts and a bioinspired approach to trail-blaze a new path to seismic isolation. We develop a novel seismic isolator whose unit cell is formed by linkages that replicate the bones of human limbs. Deformable tendons connect the limb members to a central post carrying the vertical load, which can slide against the bottom plate of the system. While the displacement capacity of the device depends only on the geometry of the limbs, its vibration period is tuned by dynamically stretching the tendons in the nonlinear stress-strain regime, so as to avoid resonance with seismic excitations. This biomimetic, sliding-stretching isolator can be scaled to seismically protect infrastructure, buildings, artworks and equipment with customized properties and sustainable materials. It does not require heavy industry or expensive materials and is easily assembled from metallic parts and 3D-printed components.

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1 Introduction

In the event of earthquakes, seismic isolation offers an effective strategy to ensure the safety of people and the prevention of damage to structures, machinery and equipment [1-6]. The most widespread seismic isolators currently on the market use elastomeric or friction-pendulum bearings [7,8]. These devices partially or completely disconnect the portion of the 'superstructure' above them from the ground motion. As a result, the fundamental vibration period of the structure is significantly increased, avoiding resonance with high-frequency content seismic excitations [9]. Seismic isolators offer different levels of damping [10], which is useful for dissipating energy and reducing the amplitude of lateral displacements during earthquakes. The inherent limitations of currently available isolators include their confined operational frequencies, manufacturing complexity, need for advanced technical expertise and substantial costs.

While elastomeric bearings are still widely used and appreciated for their simplicity and consistent performance, even after several decades in service [11–13], the friction-based devices become quickly the technology of choice when the displacement demand increases significantly. Sliding bearings generally imply a more

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complex behavior of the isolated structure, due to the intrinsic complexity of the frictional phenomena and the still limited data about the durability of their critical components [14]. The choice of the appropriate technology for seismic isolation interventions on existing or new structures requires a careful analysis [1,15]. However, even the simplest implementation of the seismic isolation technology offers a major improvement in terms of level of seismic protection of buildings and infrastructures in both industrialized and developing countries. Residential and rural buildings [16], equipment in hospitals and essential buildings [4,5], artworks in museums [6] and critical industrial facilities are nowadays often protected through many variations and combinations of seismic isolators. The considerable high cost and the perceived complexity of such devices, together with local availability constraints, often discourage a larger use of this reliable technology, particularly in less developed countries. The scientific community senses the need to create the conditions for a broader field of applications, and in this sense several low-cost solutions for seismic isolators have been proposed in the literature and are currently under investigation [4, 16–19].

The use of architectured material concepts to design next-generation seismic isolators deserves special attention, in consideration of the exceptional properties these systems exhibit in different fields of mechanics, robotics and acoustics [21-27]. This is due to an optimized geometric design of the internal structure [20,21] that can be conveniently manufactured using 3D printing at different scales [28–30]. Seismic metamaterials have been successfully proposed to protect buildings from seismic waves by creating shields around the structure through Bragg-scattering structured soils, buried mass or above-surface resonators, auxetic and hierarchical materials [31–36]. The periodicity of these media is often at the meter scale, which makes them not suited for use as seismic isolators. The employment of confined pentamode lattices as smallamplitude vibration attenuation devices has been the subject of recent discussion in the literature [37].

Ever since Leonardo da Vinci's pioneering anatomic studies [38], the mechanics of human and animal locomotion has attracted researchers' attention. Animals adjust their muscle contraction frequencies to reach a state of resonance with pendulum- and elastictype oscillation mechanisms during locomotion [39]. This frequency tuning process produces motion at low energy consumption. The bones of the legs and arms behave as pendulum systems that the muscles bend periodically so as to match their natural frequencies [40,41]. Animals such as jellyfish tune vibration frequencies through the elasticity of their tissues, which is a nonlinear function of the deflection of the mesoglea bell [39].

This work takes a novel approach to a bio-inspired design of seismic isolation systems. We design a hybrid sliding-stretching isolator (SSI) combining finite kinematics linkages that replicate the bones of human arms and legs, stretchable membranes that mimic the action of the muscle-tendon complex and confinement plates. The proposed device dissipates mechanical energy via friction and the hysteretic recentering force of the tendons. Its displacement capacity can be finely tuned through an optimized design of the geometry of the limb members, while dissipative effects can be adjusted for the application at hand by playing with the geometry, the training cycles and the material of the tendons. The SSI can be manufactured on-site or in a fabrication laboratory using 3D printers and metallic parts provided by local metal framing companies or online suppliers, and hence does not require heavy industry or expensive materials.

2 Materials and methods

2.1 Unit cell design

An exploded view of the unit cell of the SSI is shown in Fig. 1. It is composed of four articulated 'limb' members (arms and legs) branching out from a central post connected to the top plate of the device. This plate carries the vertical load transmitted by the superstructure, consisting, e.g., of a column, a bridge beam, machinery or an artifact that needs to be isolated from the foundation. A cap screwed to the top plate covers the central post, which cap can exhibit relative rotations with respect to the post, due to a deformable cap cushion positioned between these parts. Such a movement allows the top plate to achieve the correct level (Fig. 1). If rocking motions need to be prevented [5], the cushion can be removed, with the cap and the post forming a single element. The central post ends with a slider made of a low-friction material built into a recess in its base. As Fig. 1 illustrates, four corner posts are screwed to the bottom plate and connected to the limb members at



Fig. 1 Exploded view of the SSI unit cell

the ends opposite the central post. Vertical hinges connect the limbs to one another and to the posts, while four membranes-tendons connect the corner posts to the central post (see Fig. S1 and the mounting tutorial provided in Movie S1). The tendons are made of a material that can carry large stretching strains and that dissipates energy through hysteretic response [43,44]. The undeformed configuration of the limbs, depicted with red dashed lines in Fig. 2a, shows lower arms and legs with axial length a_1 , upper arms and legs with axial length a_2 , and the relative angle between these members equal to $\pi/2 + \beta$. Interestingly, the design variable β ('initial foot angle' or 'rest angle' of the limbs) can be easily varied by changing the screw points of the corner posts on the bottom plate.

The kinematics of the unit cell is described by the two parameters illustrated in Fig. 2a, for a given direction of the displacement of the central node (relative to the foundation): the angle α formed by such a direction with the horizontal axis, and the scalar projection u of the displacement vector of the central node in this direction. The displaced positions of the elbow and knee joints are easily found at the intersection points of the circle with radius a_2 , which is centered at the current position of the central post, and the circles with radius a_1 centered at the corner posts. Due to symmetry, the kinematics of the cell is comprehensively studied by assuming u > 0 and letting α vary in the interval [0, 90] deg (see Supplementary Text for analytic results). It is safe to assume that the design value of the lateral displacement allowed by the biomimetic isolator, hereafter referred to as 'displacement capacity' d, must be sufficiently lower than the minimum value of *u* producing a 'locking' configuration of the unit cell $(u = u_{lock})$. The locking condition is achieved when one or more tendons overlap the adjacent limb members (see Fig. 2b; Fig. S4 and Movie S2).

The plot in Fig. 2b shows the variation of the dimensionless locking displacement $\bar{u}_{lock} = u_{lock}/a$ with α , for $a_1 = a_2 = a$. One observes that the minimum value of \bar{u}_{lock} is attained at $\alpha = \pi/4 - \beta/2$, and that such a value grows appreciably when the rest angle changes from positive to negative. Indeed, it increases from 0.468 to 0.714 (\approx 53%) when switching β from 10 deg to -10 deg. It is also possible to double the displacement capacity of the device by stacking 2 unit cells one over the other in the vertical direction, as shown in Fig. 2c (see also Fig. S2, D). The remarkable increase in d in systems with negative rest angles is achieved without changing the limbs' length and actually slightly reducing the footprint of the device (see insets in Fig. 2b). Overall, the displacement capacity depends only on the geometric design variables a_1, a_2 and β (see also Movie S2).

Positive values of the rest angle are needed to build periodic systems formed by arrays of unit cells, since the knee/elbow joints of adjacent cells do not touch one another if β is sufficiently greater than zero (Fig. S2, B). This design approach distributes the vertical load *P* transmitted by the superstructure among multiple central posts, creating a periodic metamaterial.

The bio-inspired character of the proposed seismic isolator is multifold. First, the shape of the unit cell replicates that of a human body with bent arms and legs (Figs. 1, 2 and 3). Second, the tendon-membranes' capacity to stretch acts as a recentering mechanism of the central post, which regulates the fundamental vibration period of the isolated structure. The extension-andrelease working principle of the membranes produces time fluctuations of kinetic and stored energies similar to those induced by the stretching and recoil of animals' tendons during running and hopping [40]. Such a response also converts the frequency tuning mechanism associated with the locomotion of animals [39] into a passive mode. While animals move at resonance through the active control of locomotion by muscles, tendons and tissues, the SSI analyzed in this study works in an opposite fashion: it tunes the nonlinear stiffness of the tendons to avoid resonance with seismic excitation frequencies [9]. It is also possible to actively control the isolator by equipping the device with actuated cables that run on top of the posts or along the



Fig. 2 Kinematic response. **a** Kinematics of the unit cell. **b** Locking displacements versus loading angle α and rest angle β . **c** Deformed configuration of a two-layer system (see also Fig. S2, D)

tendons controlled, e.g., by actuators embedded in the joints [42] (Fig. 2b and Fig. S2, B). This optional feature can be useful because it allows adjustment in real time of the fundamental vibration period and the dissipation capacity of the isolated structure to the earthquake frequency and energy content during extreme events [3]. The active control provides an additional recentering mechanism of the system.

2.2 Preparation of samples

Physical models of the SSI were manufactured at the Rapid Prototyping Laboratory of the University of Salerno. This was achieved using fused deposition modeling (FDM) 3D printers, a lathe from a partner metal framing company and Aluminum 7075-T651 (Ergal) confinement plates (see Supplementary Materials for details). The analyzed prototypes feature a single unit cell with the properties $a_1 = 97.0$ mm, $a_2 = 100.5$ mm, $\beta = 0$ and overall height of 95 mm (including the confinement plates). The non-structural components were 3D printed using eco-friendly polylactic acid (PLA) filaments. The load-carrying members of the tested prototypes were fabricated in S235 steel through a parallel lathe (Fig. S1). The slider underneath the central post (Fig. 1) is a circular disk made of

polytetrafluoroethylene (PTFE). One of the tested prototypes (prototype #1) does not have tendons and was analyzed to study the pure-friction sliding response of the central post (Fig. 3a). Prototype #2 features tendons 3D-printed using a thermoplastic polyurethane (TPU) filament for FDM (Fig. 3d and Movie S3). Prototypes equipped with fully 3D-printed unit cell parts were also manufactured for demonstrative purposes (Fig. 3a,b and Movie S3). Table S1 of Supplementary Text illustrates the key manufacturing parameters of the biomimetic isolator prototypes.

2.3 Experimental validation procedure

Experimental validation tests were designed 'ad hoc' in collaboration with FIP MEC srl, a leading company in the field of antiseismic devices based in Padova (Italy). A loading frame equipped with vertical and horizontal hydraulic actuators (Fig. S3) was employed to apply unidirectional displacement histories to the bottom plate, while subjecting the top plate to a fixed vertical load P.

The testing activities led to the execution of 1 training cycle and 4 additional cycles of a sinusoidal displacement time-history with a frequency of 0.40 Hz and amplitude $d = \pm 50$ mm. Additional tests were run



Fig. 3 Physical models and experimental validation. **a** Motion animation of a demonstrative version of prototype #1 equipped with fully 3D-printed unit cell parts, which can be moved by hand. **b** Demonstrative version of prototype #2 equipped with

telescopic tendons (see Movie S3 for a motion video-clip). (c) Prototype #2 with stretchable tendons and metallic posts under testing (a featured video is given in Movie S4)

by applying one training cycle and 4 additional cycles of triangular displacement histories with frequency of 0.50 Hz and amplitude $d = \pm 25$ mm. Three different values of the vertical load were applied to the top plate (P = 5, 15, 25 kN, see Movies S4–S10). Two sets of tendons were analyzed (sample #2): unconditioned tendons, and tendons subject to preliminary stretching through a few percent axial strains, leading such members to a state of pretension when the device was in the rest configuration. This pre-conditioning prevented the occurrence of significant residual strains after the training cycle (see Sect. 4). For P = 5 kN, two pre-conditioned tendons were placed on opposite edges with respect to the loading direction, while the remaining two tendons were mounted as unconditioned (so that there was always one pre-conditioned tendon active for positive and negative lateral displacements). For P = 15 kN, three pre-conditioned tendons were mounted, while for P = 25 kN, all the tendons were pre-conditioned. The maximum engineering strain suffered by the tendons was estimated to reach values as high as 28% under testing, while the engineering strain rate suffered by the tendons was estimated to reach a peak value of 0.65/s. The applied load frequencies are consistent with the typical frequency range of seismically isolated buildings [2,3]. To subject the tested specimens to similar sliding conditions, sample #1 was obtained by cutting and removing the membranes from sample #2, after all the tests on this sample were completed. Preliminary mechanical characterization tests were run on the tendons, as detailed in Supplementary Text.

3 Mechanical modeling

3.1 Nonlinear force-displacement response

The cyclic uniaxial tension tests on the tendons presented in Supplementary Text are well described by the pseudo-elastic (PE) constitutive models by Dorfmann and Ogden for rubber-like materials [43,44]. Let λ and $\hat{\sigma}_t$, respectively, denote the stretch ratio (after pre-conditioning) and the nominal stress carried by the tendons. Assuming a no-compression behavior (due to the thin-walled cross section), we model the tensile response of the tendons through the 'model 2' analytically described in Supplementary Text (PE model), at the strain rate of 0.11/s and up to $\approx 30\%$ incremental strains from the pre-conditioned state. The maximum strain rate of 0.65/s observed in the tendons of sample #2 under testing is significantly higher than that characterizing the cyclic tests on the tendons presented in Supplementary Materials. It has been reported in the literature that an increase in the strain rate may appreciably harden the stress-strain curve of TPU during

the loading phase [45,46], while keeping the unloading branch essentially unchanged [45]. In order to account for high-strain-rate effects, we multiply the PE function $\hat{\sigma}_t(\lambda)$ by a scaling factor $(1 + \psi)$, where ψ denotes a strain rate parameter [47].

The overall restoring force F_r transmitted from the tendons to the central post (Fig. S2, C) is computed through the equation:

$$F_r = A_t \left(\sum_j (1 + \psi) \, \hat{\sigma}_t(\lambda_{t,j}) \, \hat{\mathbf{k}}_{t,j} \right) \cdot \hat{\mathbf{k}}^u \tag{1}$$

where now A_t is the cross section area of the tendons in the rest configuration ; $\lambda_{t,j}$ and $\hat{\mathbf{k}}_{t,j}$ denote the stretch ratio and the unit vector associated with the tendon that links the *j*-th corner post with the central post (j = 1, 3, 7, 9, see Fig. S2, A), respectively; and $\hat{\mathbf{k}}^u = \{\cos(\alpha), \sin(\alpha), 0\}$ indicates the unit vector in the direction of the applied displacement *u*. The no-compression assumption implies $\hat{\sigma}_t = 0$ for any $\lambda_{t,j} < 0$.

A second horizontal force F_f acting on the central post follows from the friction resistance opposed by the slider-plate interface to the sliding movement (Fig. S2, C). The constitutive law for F_f can be obtained by generalizing the nonlinear friction model for concave sliding bearings by Lomiento et al. [8] to the SSI. Such a model assumes that the friction coefficient μ reduces its value with increasing values of the applied vertical load P ('load' effect); varies with the sliding velocity $v = \dot{u}$ ('velocity' effect); slightly reduces under cycling loading ('cycling' effect); and sharply increases when the motion initiates or reverses its direction ('breakaway' effect). The experimental results presented in Fig. 4 highlight that the model by Lomiento et al. [8] can be reasonably applied to the SSI samples under examination by discarding the cycling and breakaway effects. We are therefore led to the following constitutive law for F_f :

$$F_f = \mu P \operatorname{sign}(v) \tag{2}$$

where v is the sliding velocity, sign(·) denotes the signum function, and it results in:

$$\mu = \mu_{s0} e^{-\frac{p}{p_{ref}}} \left(\gamma + (1 - \gamma) e^{-\frac{|\nu|}{v_{ref}}} \right).$$
(3)

Here, μ_{s0} indicates the slow-motion coefficient of friction under zero vertical load; P_{ref} and v_{ref} denote reference values of the applied vertical load *P* and sliding velocity, respectively; and γ denotes a dimensionless scalar parameter greater than one [8].

3.2 Effective dynamic properties

We denote energy dissipated per cycle by the SSI through the symbol EDC. An effective value of the dynamic friction coefficient of prototype #1 can be defined as follows:

$$\mu_{eff} = EDC/(4Pd). \tag{4}$$

Let now F_d denote the value of the base shear force F corresponding to the design displacement u = d of prototype #2. We compute the effective damping coefficient of this prototype through the following formula provided by international standards for seismic isolators [10]:

$$\xi_{eff} = \frac{EDC}{2\pi F_d d}.$$
(5)

The effective period of vibration of the system is instead computed as follows:

$$T_{eff} = 2 \pi \sqrt{\frac{M}{F_d/d}}.$$
(6)

M = P/g being the mass of the superstructure (here *g* denotes the gravitational acceleration). The above properties control both the extreme values of the seismic load suffered by the superstructure and the displacement drift between the superstructure and the foundation [48]. They are employed to characterize the fundamental performance target of the isolated building and to perform the selection of the appropriate isolation system in the pre-design phase [1]. The fine-tuning of the isolation system requires a detailed structure and the seismic isolators, which accounts for the accurate modeling of the force–displacement response described in the previous section.

4 Results and discussion

Let $F = F_r + F_s$ denote the overall shear force acting on the top plate of the SSI (base shear of the superstructure). The experimental and theoretical results obtained for the shear force F vs. lateral displacement u response of prototype #1 and #2 are illustrated in Figs. 4 and 5, respectively, in correspondence with the examined values of the vertical load (P = 5, 15, 25 kN). A trial and error procedure was employed to obtain the best fit parameters of the friction model described by Eqs.



Fig. 4 Shear force F versus lateral displacement u response of the SSI prototype #1. Comparison of experimental results and theoretical predictions under fixed vertical load P and cyclic displacement histories with amplitude $d = \pm 50$ mm, for P = 5 kN a,b); P = 15 kN c,d; and P = 25 kN (e,f). The displacement

window of triangular loading tests has been restricted to 85% of the maximum value to exclude disturbance effects related to load reversal. Error bars refer to deviations of the shear force from the mean value under cyclic loading. Video recordings of selected tests are given in Movies S5–S7

(2–3) and the constitutive model given by Eq. (1) with respect to the experimental results for prototypes #1 and #2, respectively (after the training cycles). We estimated $P_{ref} = 42.35$ kN, $\mu_{s0} = 0.47\%$, $\gamma = 4.00$, $v_{ref} = 2.50$ mm/s and $\psi = 0.19$. The accuracy of the employed mechanical models for F_f and F_r is demonstrated by the good theory vs. experiment matching observed in Figs. 4 and 5.

For the tests run on prototype #1, we note the following theory vs. experiment differences in terms of the average energy dissipated per cycle (sinusoidal tests): -5.27 % for P = 5 kN (theory: 16.61 J; experiment: 17.54 J); 11.07% for P = 15 kN (theory: 39.36 J; experiment: 35.44 J); and 7.86% for P = 25 kN (theory: 51.81 J; experiment: 48.03 J). These values of *EDC* correspond to average values of μ_{eff} varying from 1.66% (P = 5 kN) to 1.04% (P = 25 kN). The oscillations of the experimental results visible in Fig. 4 are explained by accuracy measurement errors due to the low values of the shear forces recorded during the tests (0.1–0.3



Fig. 5 Shear force *F* versus lateral displacement *u* response of the SSI prototype #2. **a** Images of the tendons reinforced with M3 bolts at the extremities. **b** Components of the adopted mechanical model (sinusoidal loading with P = 25 kN). **c**-**h**) F - u curves for P = 5 kN (**C**,**D**); P = 15 kN (E-F); and P = 25 kN (**g**-**h**).

The displacement window of triangular loading tests has been restricted to 85% of the maximum value to exclude disturbance effects related to load reversal. Video recordings of selected tests are given in Movies S8–S10

kN), which are close to zero on the scale range of the horizontal actuator (0-100 kN), and the experimentally measured variability of the vertical load P. Passing to examine the sinusoidal test on sample #2 under P = 5kN, we note that the loading branches of the experimental F - u response exhibit low-slope segments in proximity to the points with u = 0 (see Fig. 5c). Such portions of the F - u curve are caused by the fact the unconditioned tendons are initially 'slack' due to the residual strains accumulated in the training cycle (see also Movie S8). In the tests with P = 15 kN, the initial slope of the F - u curve (near u = 0) is smaller for u > 0 than for u < 0, thanks to the insertion of two preconditioned tendons working for u < 0 and only one working for u > 0 (Fig. 5e and Movie S9). Finally, for P = 25 kN all the loading branches of the F - u curve exhibit considerably high slope near u = 0, due to the fact that all the tendons were pre-conditioned in correspondence to such a value of P (Fig. 5g and Movie S10). As a result, the overall matching between theoretical predictions and experimental observations of the force-displacement response is appreciably more accurate for P = 25 kN than for the previous cases (cf. Fig. 5c,e,g).

Let us now compare the results of sinusoidal tests, affected by material- and friction-dependent nonlinearities (due to the time-variation of the sliding-velocity of the central post), with those of triangular input tests, where the sliding velocity is constant (see Figs. 4, 5). A comparative analysis of the response laws given in Figs. 4 and 5 reveals that the nonlinearity of the F - ucurve of prototype #2 is essentially due to the nonlinear behavior of the tendons and pre-conditioning effects. The hysteretic response of the tendons determines the different shapes of the loading and unloading branches shown in Fig. 5d,f,h [43-45]. A featured video of the deformation of the tendons of prototype #2 under testing (P = 25 kN) is given in Movie S4, while video recordings of the sinusoidal tests on prototypes #1 and #2 are provided in Movies S5–S10. Referring to the theoretical model for prototype #2, we record $\xi_{eff} =$ 17.05%, 24.72%, 27.84% for *P* = 5kN, 15 kN and 25 kN, respectively. Similarly, we estimate T_{eff} of prototype #2, respectively, equal to 1.32 s, 2.09 s and 2.51 s for P = 5kN, 15 kN and 25 kN. For P = 25 kN, the employed mechanical model estimates $T_{eff} = 1.94$ s $(\xi_{eff} = 20.87\%)$ when setting the cross section area of the tendons A_t to twice the value A_{t_0} corresponding to prototype #2 (cf. Fig. 3e).



Fig. 6 Force–displacement responses of prototype #2 for variable sizes of the tendons (P = 25 kN)

5 Scaling procedure

We will now extrapolate the results obtained in the previous section to SSIs of different sizes and loaddisplacement capacities. It is easy to recognize that the load carrying capacity of the SSI prototypes can be adequately increased by playing with the diameters of the central post, central cap, central cushion and slider: a load carrying capacity of 250 kN, e.g., requires the adoption of a central post with a \approx 41-mm diameter, and a PTFE slider with a \approx 95-mm diameter, when using the same materials of prototypes #1 and #2 [49]. Alternatively, one can employ an array configuration (Fig. S2, B) to distribute the vertical load among smaller-size multiple posts, as we have already noticed. For what concerns the displacement capacity, it is possible to reach d = 500 mm using a one-layer system with limbs' length $a \approx 710$ mm or a two-layer system with $a \approx 355$ mm.

The scaling law of the tendons can be obtained via the following formula inspired by international standards for seismic isolators [50]:

$$F_{r_d}(P) = \chi P \tag{7}$$

where F_{r_d} denotes the design value of the restoring force to be carried out by the tendons, and χ is a dimensionless parameter. The 2001 California Building code [51] prescribes a minimum value of the post-elastic stiffness of a nonlinear isolation system such that the corresponding restoring force can be computed through the above formula with $\chi \ge 0.05$. The AASHTO code for seismic isolation [52] instead recommends $\chi \ge 0.025$ (in association with a suitable limitation of the fundamental period of the device, see [50] for further details). It is worth noting that the maximum value of the engineering strain that can be suffered by the tendons, in correspondence to the locking configuration (ϵ_{lock}), is independent of the limbs' length, which implies that such a quantity is also independent of the displacement capacity d, for a given value of β . Referring, e.g., to the case with $a_1 = a_2 = a$ and $\beta = 0$, we observe that ϵ_{lock} is equal to $\sqrt{2} - 1$, independent of the value of a (see the Mathematica[®] code given in Supplementary Materials). ϵ_{lock} increases for $\beta < 0$, reaching ≈ 0.55 for $a_1 = a_2 = a$ and $\beta = -10$ deg.

We are now in a position to generalize Eqs. (5–6) to an arbitrary SSI. We estimate ξ_{eff} and T_{eff} of such a device through:

$$\xi_{eff} = \frac{2\lambda\mu_{eff}}{\pi(\mu_{eff} + \chi)},\tag{8}$$

$$T_{eff} = 2\pi \sqrt{\frac{d}{(\mu_{eff} + \chi)g}} \tag{9}$$

where λ is a scalar parameter defined by the ratio between the *EDC* of a SSI equipped with tendons and that of the same device without the tendons. It is seen that the design variables T_{eff} and ξ_{eff} depend on the geometry of the device, the current value of μ_{eff} , the ratio χ between the design value of the recentering force of the tendons and the maximum vertical load, and the dimensionless parameter λ , which characterizes the energy dissipation capacity of the tendons (we recorded λ variable between 1.87, for P = 5 kN, and 1.34, for P = 25 kN, during the tests run on prototype #2).

The dynamic properties of the SSI can be effectively adjusted for the particular application at hand. Setting $\mu_{eff} = 2.0\%$, we estimate that T_{eff} varies from 1.66 s ($\xi_{eff} = 11.57\%$) to 2.96 s ($\xi_{eff} = 27.68\%$) when one assumes in the design phase ($d = \pm 150$ mm, $\chi = 0.20, \lambda = 2.0$) and ($d = \pm 250$ mm, $\chi = 0.095, \lambda = 2.5$), respectively. The friction coefficient can be tuned by playing with the vertical load and the size and materials of the slider and the resting plate, while the tendons' energy dissipation properties can be adjusted through their preliminary training, in addition to an optimized design of the geometry and materials. The insertion of special dissipative elements at the mid-span of the tendons and the use of recycled materials [30] can also be considered.

6 Concluding remarks

We conclude that the biomimetic isolators analyzed in this study help us to forge a novel path to seismic isolation. Such devices with an anthropomorphic character are classified as highly tunable seismic isolators that can be manufactured with customized properties using optimal geometries and sustainable materials easily available around the world. Some key advantages enjoyed by these systems over their current state-ofthe-art counterparts are derived from the possibility to tune the displacement capacity acting only on the internal architecture of the unit cell; the uniaxial tension regime of the tendons, up to 40%-55% maximum axial strains, which is suitable for a class of materials much larger than the elastomeric products employed in rubber bearings [53]; and the possibility of creating periodic 'metaisolators' (Fig. S2, B). In addition, the SSI does not require heavy industry and is easily repaired by replacing the tendons after an extreme seismic event.

It is worth noting that the level of preliminary training of the tendons can be employed as a peculiar design variable of the SSI. We have observed that the reduced slope at the origin of the hysteretic loops of the device indicates a prevalent contribution of the frictional component to the base shear. By adjusting the amplitude of the pre-conditioning of the tendons one can suitably design the extension of this region of reduced reaction force. With such a design flexibility the building movement can be facilitated at the onset of the earthquake excitation, preventing the experience of significant levels of acceleration transferred to the structure, while providing higher stiffness for larger displacements.

The design and testing of architectured seismic isolators that feature an independently tunable antiseismic performance against horizontal and vertical ground motions will be addressed in future work, employing, e.g., linkages that mimic the knee articulation of the human leg in the vertical plane. Such a nonconventional performance is highly desirable in the case of high-risk industrial installations and power plants [5].

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Author contributions G.W.M. formulated the initial concept of the isolator without the tendon elements. F.F. added the tendon members to the isolator concept and led the writing of the manuscript. G.B. included friction effects and designed and directed the experiments together with F.F. N.S. led the computeraided design and the manufacturing of the final isolator prototypes. A.A. was in charge of the mechanical modeling of the experimental results. All authors analyzed the results of the experimental tests and reviewed the manuscript.

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Data Availability Statement The Mathematica[®] code employed for the prediction of the kinematics of the biomimetic isolator is available as an Appendix to Supplementary Text. The stereolithography (STL) files of all the unit cell parts of the demonstrative prototypes can be provided by the corresponding author upon request.

Declarations

Conflict of interests The authors declare that they have no conflict of interest.

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